Joint Search for Muon Neutrino Disappearance at Δm² ~ 1 eV² with SciBooNE and MiniBooNE

April 29, 2011
Fermilab Wine and Cheese Seminar
Yasuhiro Nakajima (Kyoto U./LBNL)

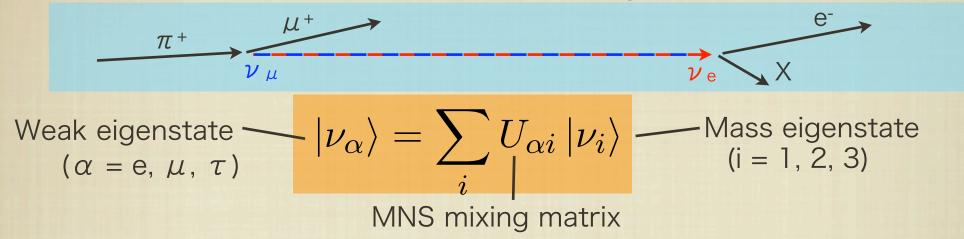
- Introduction
 - Neutrino oscillation
 - Short-baseline ν_{μ} disappearance
- Experiments: SciBooNE and MiniBooNE
- SciBooNE-MiniBooNE joint ν_{μ} disappearance analysis
- Results

Introduction

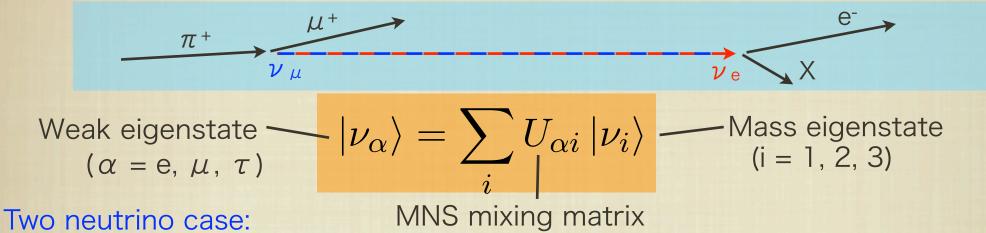
Neutrinos can change their flavors if neutrinos have finite masses and if the weak and mass eigenstates are mixed



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 $P(\nu_{\alpha} \to \nu_{\beta}) = |\langle \nu_{\beta} | \nu(t) \rangle|^2 = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 [\text{eV}^2] L[\text{km}]}{E[\text{GeV}]} \right)$

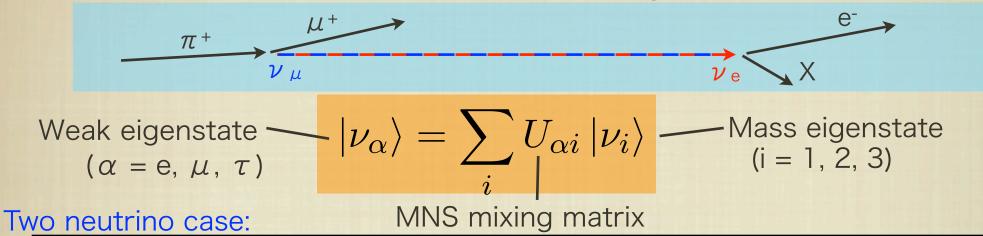
 θ : mixing angle

 Δm^2 : mass squared difference

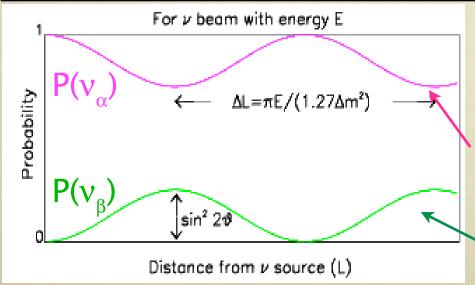
L [km] : the distance traveled

E (GeV): the energy of neutrino

Neutrinos can change their flavors if neutrinos have finite masses and if the weak and mass eigenstates are mixed



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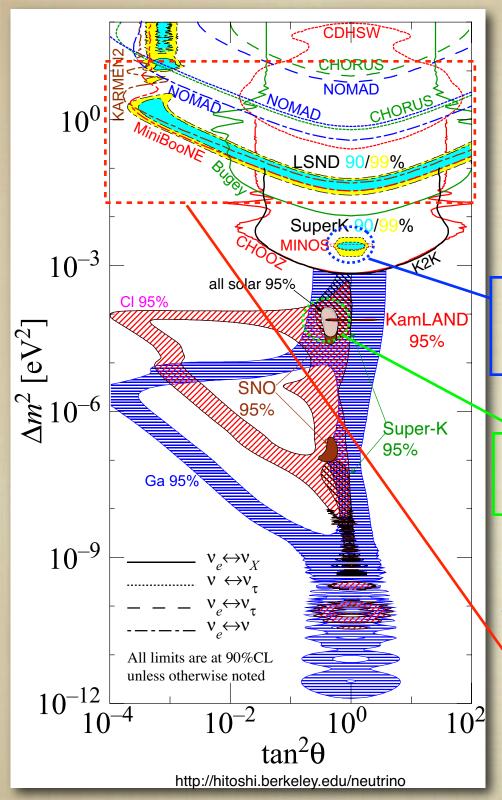
 Δm^2 : mass squared difference

L [km] : the distance traveled

E (GeV): the energy of neutrino

disappearance of ν_{α}

appearance of ν_{β}



Observed Neutrino Oscillations

- Atmospheric region: $\Delta m^2 \sim 10^{-3} \text{ eV}^2$
 - Super-K, K2K, MINOS, etc
- Solar region: $\Delta m^2 \sim 10^{-5} \text{ eV}^2$
 - SNO, Super-K, KamLAND, etc

Only 2 Δm^2 regions are allowed in the current

SM with 3 neutrino generations
However, there is one more region claimed by the LSND experiment at $\Delta m^2 \sim 1 \text{ eV}^2$

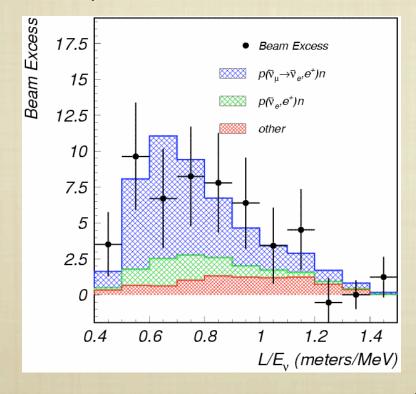
The LSND Signal

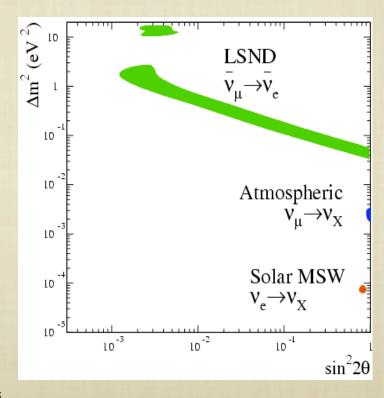
The LSND experiment observed a small excess of $\overline{\nu}_e$ evens in a $\overline{\nu}_\mu$ beam

Data excess: $87.9 \pm 22.4 \pm 6.0$ (3.8 σ)

Best fit: $\Delta m^2 \sim 1 \text{ eV}^2$, $\sin^2 2\theta \sim 0.003$

hep-ex/01014049





Active-sterile Neutrino Oscillation?

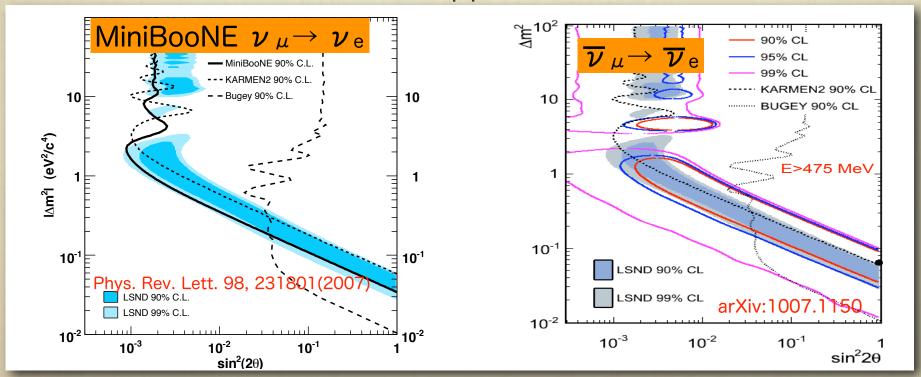
- A possible explanation of the LSND signal:
 - Oscillation with active and "sterile" neutrinos

A simple realization of the sterile neutrino is right-handed neutrino ν_R , which can be mixed with active ν_L .

3+1 sterile neutrino scheme Δm^2_{LSND} $\Delta m^2_{23} \qquad \qquad \nu_s$ ν_{τ} $\Delta m^2_{12} \qquad \qquad \nu_e$

MiniBooNE ν_e Appearance Results

- MiniBooNE experiment recently tested the LSND signal.
- Ruled out most of LSND region in $\nu_{\mu} \rightarrow \nu_{e}$ search.
- Be However, observed a data excess in $\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e}$ measurement.
 - Consistent with LSND???
- We want to test this with disappearance measurements!



Appearance vs. Disappearance

How can we test appearance signals by disappearance measurements?

$$u_{\mu}
ightarrow
u_{e}$$
 appearance $u_{\mu}
ightarrow
u_{e}
ightharpoonup = 4
u_{e4}
u$

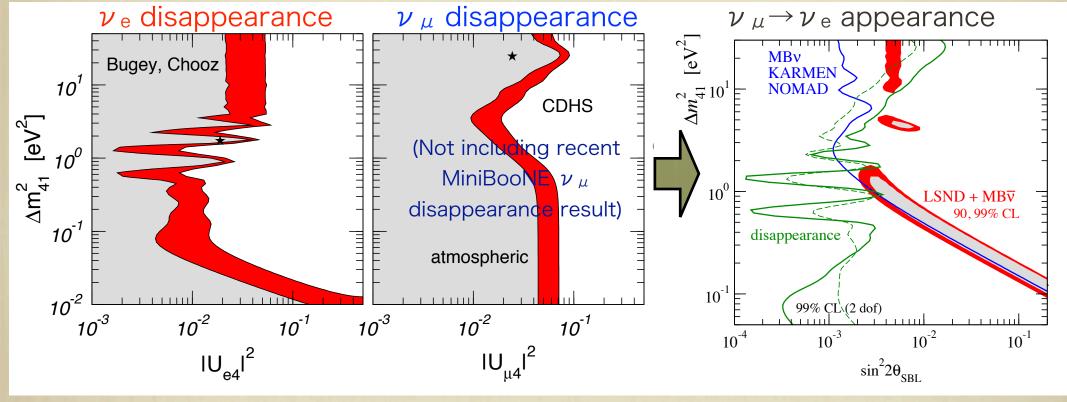
 $\nu_{\mu} \rightarrow \nu_{e}$ appearance probability can be constrained by ν_{e} and ν_{μ} disappearance measurements!

Impact of Disappearance Experiments

Compatibility of the existing measurements in (3+1) model

M. Maltoni, J. Conf. Ser. <u>110</u>, 082011 (2008)

J. Kopp, M. Maltoni, T. Schwetz, arXiv:1103.4570



- LSND allowed region is incompatible with disappearance results.
- Disappearance measurement is a powerful tool!

Other Scenarios

3+2 sterile neutrino mixing

PRD <u>76</u>, 093005 (2007) PRD <u>80</u>, 073001 (2009) arXiv:1103,4570

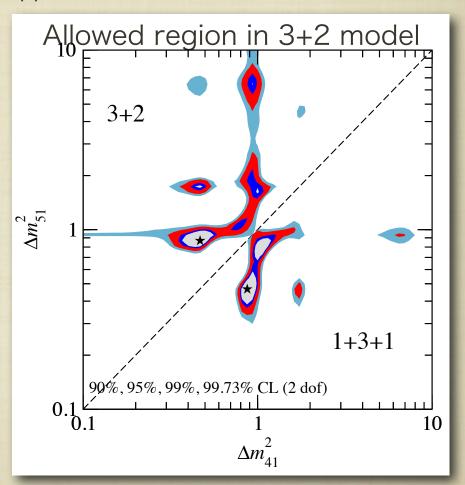
Sterile neutrinos in extra dimensions

PRD <u>72</u>, 095017 (2005)

- Decaying sterile neutrino JHEP <u>09</u>, 048 (2005)
- CPT violationPRD <u>77</u>, 033001 (2008)

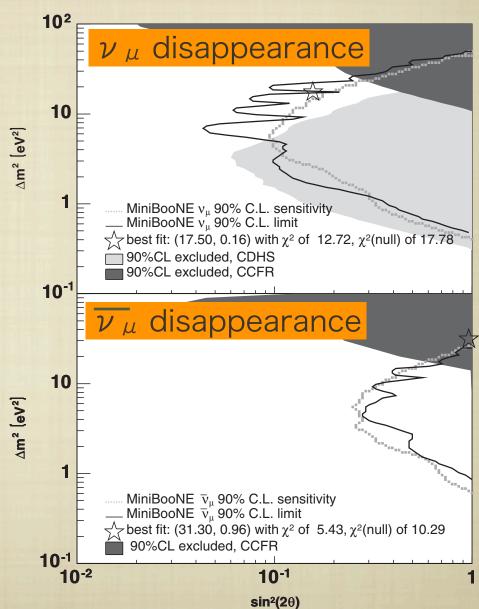
Disappearance measurements can constrain these models.

J. Kopp, M. Maltoni, T. Schwetz, arXiv:1103.4570



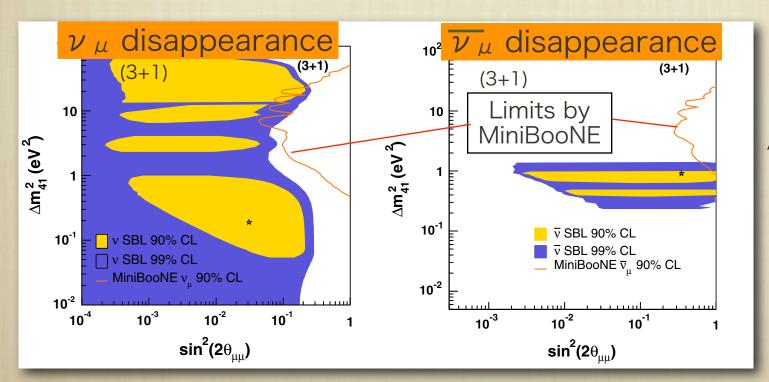
ν_μ Disappearance Measurements

- Important to test ν_{μ} and $\overline{\nu}_{\mu}$ disappearance independently.
 - Testing CPT-invariance.
- Recently, MiniBooNE searched for ν_{μ} and $\overline{\nu}_{\mu}$ disappearance with MiniBooNE data only (PRL 103, 0611802)
- This analysis used the flux shape only, and suffered from large flux and cross section uncertainties.



νμ Disappearance Measurements (cont'd)

- Large allowed region from a global fit to world existing data with the (3+1) model, if we fit ν_{μ} and $\overline{\nu}_{\mu}$ independently.
- Why don't you improve MiniBooNE results with a near detector (SciBooNE).
 - Flux+shape analysis with reduced systematic error.



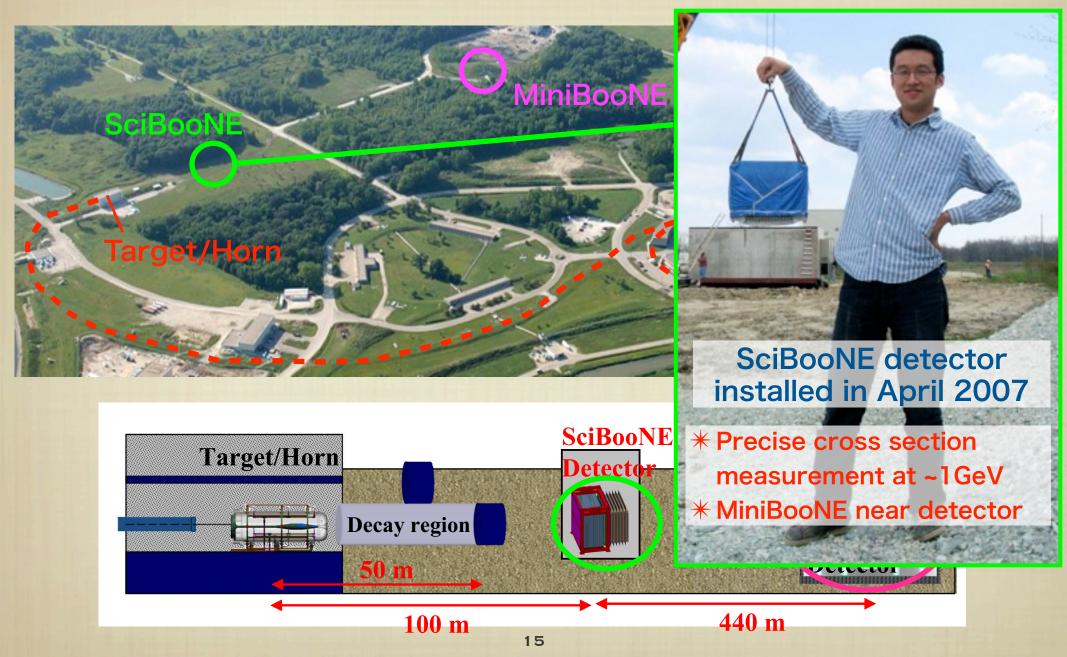
Allowed regions from (3+1) global fits

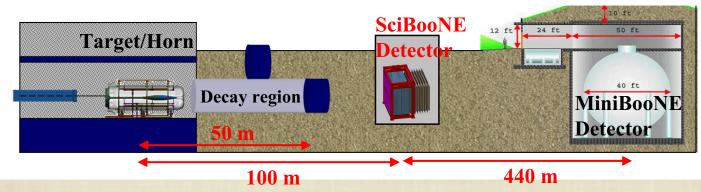
G. Karagiorgi, et al. Phys. Rev. D **80**, 073001 (2009)

Experiments









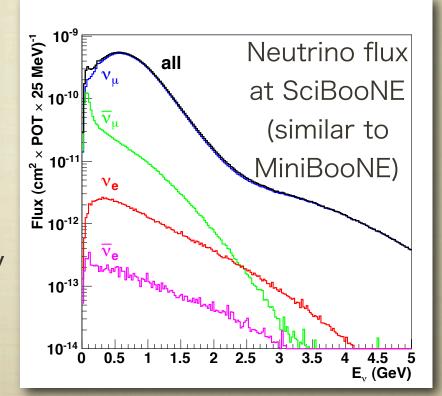
- MiniBooNE experiment (2002) is designed to test the LSND signal at L/E ~ 0.7 meter/MeV
 - L/E for MiniBooNE: 540m / 0.8 GeV ~ 0.7 m/MeV
- SciBooNE experiment (2007-2008) has two purposes
 - Precise measurement of neutrino cross section for future oscillation experiments (T2K, etc)
- Common beamline + Common neutrino target (both carbon)

 Significant reduction of systematic errors

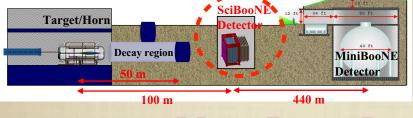
Fermilab Booster Neutrino Beam

Be target and horn 50m decay volume soil π^+ proton π^+ ν_μ

- Intense ν_{μ} beam with the mean energy of ~0.8 GeV
 - 93% pure ν_{μ} beam.
- Anti- ν_{μ} beam is also produced by inverting horn polarity.

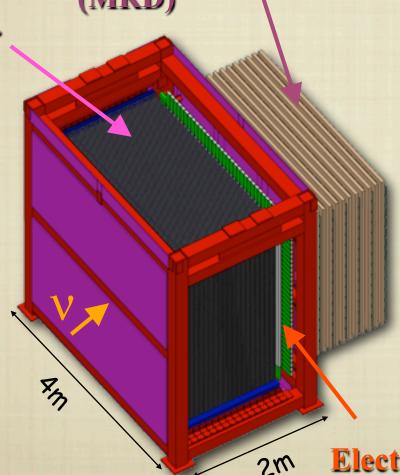


SciBooNE detector



Muon Range Detector (MRD)

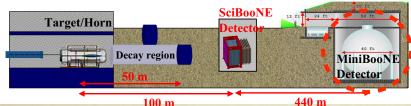


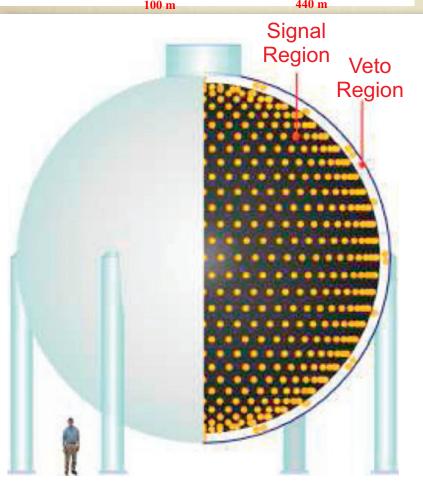


- Located at 100 m from target.
- SciBar:
 - Fully active scintillator tracker (~14000 strips)
 - Neutrino target (~10 ton)
 - Main component : CH
- Muon Range Detector (MRD)
 - A sandwich type detector of steel + plastic scintillator.
 - Reconstruct muon momentum from its pathlength

Electron Catcher (EC)

MiniBooNE detector



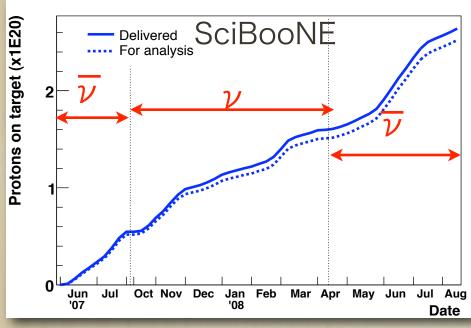


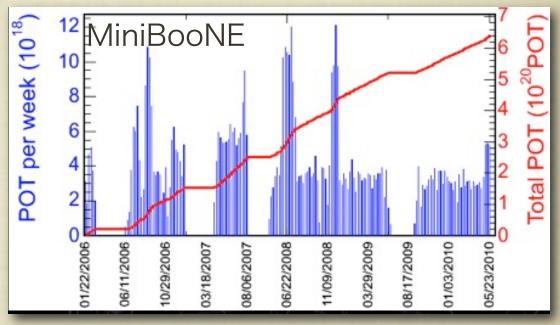
- Located at 540 m from target
- Mineral oil Cherenkov detector
 - n = 1.47
 - Select ν_{μ} by single muon and its decay-electron signal.
 - Total mass: ~800 ton
 - Main component: CH2
- Taking beam data since 2002

2 detectors share the beam and the target material (both carbon)

Data sets

	Period	BNB Mode	SciBooNE POT	MiniBooNE POT
(Sep. 2002 - Dec. 2005	Neutrino		5.58×10^{20}
	Jan. 2006 - Aug. 2007	Antineutrino	$0.52 \times 10^{20} \text{ (from Jun. 2007)}$	1.71×10^{20}
	Oct. 2007 - Apr. 2008	Neutrino	0.99×10^{20}	0.83×10^{20}
	Apr. 2008 - present	Antineutrino	1.01×10^{20} (until Aug. 2008)	ongoing





Analysis of the full neutrino data sets is presented

- SciBooNE: 0.99 x 1020 POT
- MiniBooNE: (5.58 + 0.83) x 10²⁰ POT

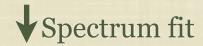
Analysis

Analysis Overview

Two independent analyses

Spectrum fit

SciBooNE data



CC interaction rate measurement



MiniBooNE rec. E_v prediction



Oscillation Fit

MiniBooNE rec. E_v data

Advantage:

Decouple oscillation fit from constraint.

Observe the amount of constraint.

Simultaneous fit

SB + MB Rec. E_v Data



Oscillation Fit

SB + MB Rec. E_v Prediction

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Direct fit for disappearance in SciBooNE and MiniBooNE. Correlation between the two constrain systematic error.

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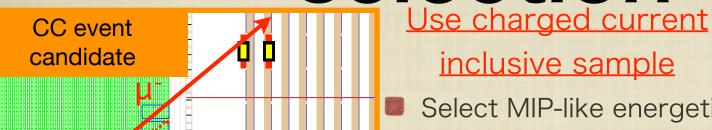
SB + MB Rec. E_v Prediction

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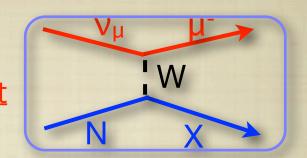
Direct fit for disappearance in SciBooNE and MiniBooNE. Correlation between the two constrain systematic error.

SciBooNE event

selection

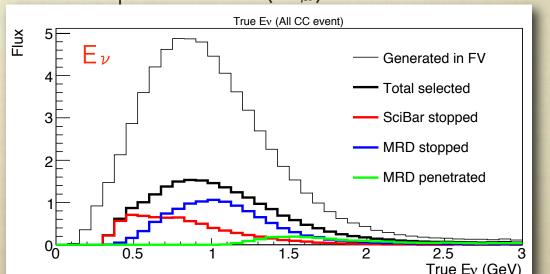


MRD



- Select MIP-like energetic tracks (P_{μ} >0.25GeV)
- Reject side-escaping muons.
- 3 samples:
 - SciBar-stopped (P_{μ}, θ_{μ})
 - MRD-stopped (P_{μ} , θ_{μ})
 - MRD-penetrated (θ_{μ})

 P_{μ} : Muon momentum reconstructed by its path-length $\theta \mu$: Muon angle w.r.t. beam axis



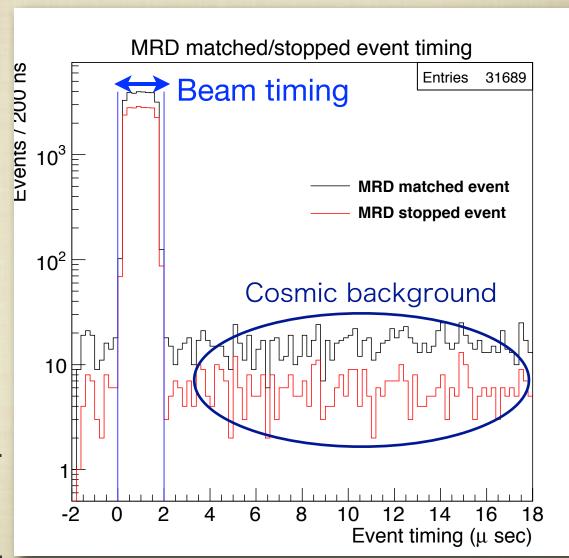
EC

SciBar

SciBar

Neutrino event selection

- Booster provide pulsed beam with 1.6 μ sec width.
- Require the event timing to be within the 2 μ sec beam timing window.
 - Less than 0.5% cosmic ray contamination.
- ~14K SciBar-stopped events.
- ~20K MRD-stopped events.
- ~4K MRD-penetrated events.



Muon distributions

2 neutrino interaction simulators are used:

NEUT: SK, K2K, T2K, etc (+ all other cross section measurements in SciBooNE)

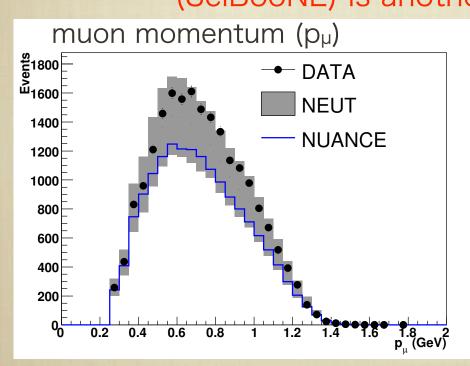
NUANCE: MiniBooNE, etc (Use NUANCE for this joint oscillation analysis)

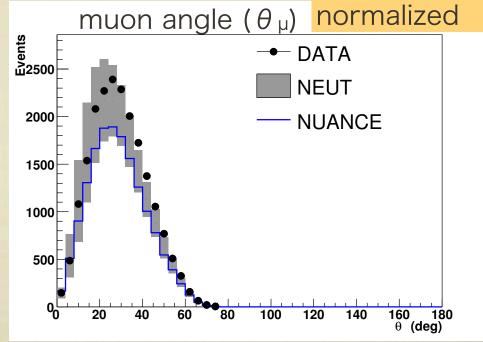
Both tuned to explain data, but predict different cross sections.

 \Rightarrow

Testing these in a single experiment (SciBooNE) is another important topic!

MRD-stopped Absolutely

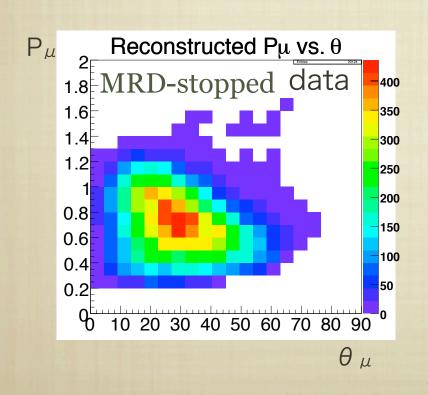


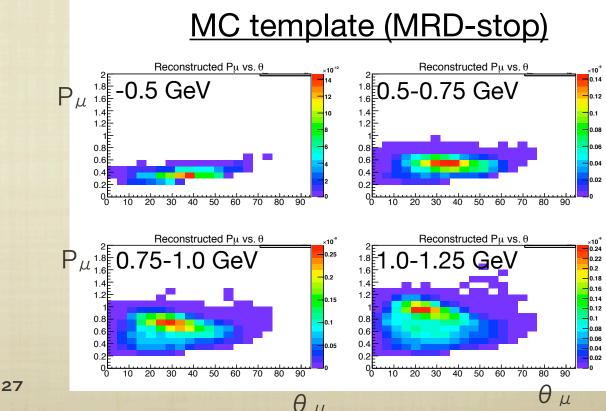


MC reproduce data within the systematic error

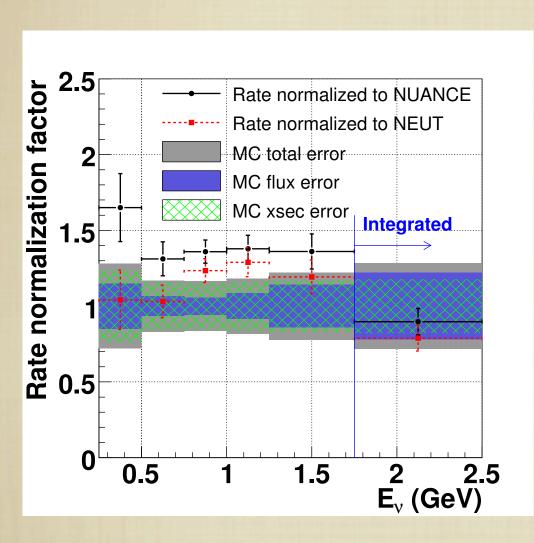
Spectrum fit

- Tune MC prediction by re-weighting as a function of true neutrino energy.
- Determine the rate normalization factor which best fits to p_{μ} vs. θ_{μ} 2D distributions.
 - All three samples (SciBar-stop, MRD-stop and MRD-penetrated samples) are used simultaneously.





CC interaction rate



Extract CC interaction rate

normalization factor # of event
$$\mathcal{R}_i = \underbrace{f_i \cdot \mathcal{N}_i^{pred} \cdot P_i}_{\text{Furity}}$$
 prediction Purity

This is product of (flux) x (cross-section)



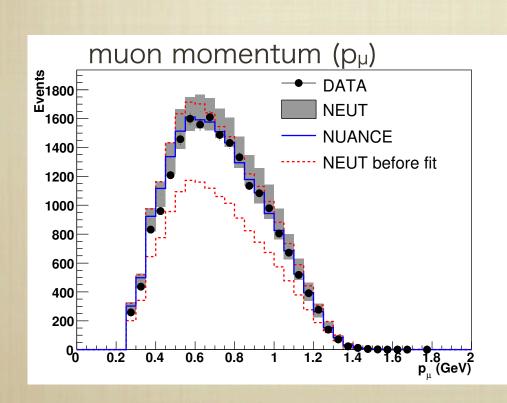
Published in

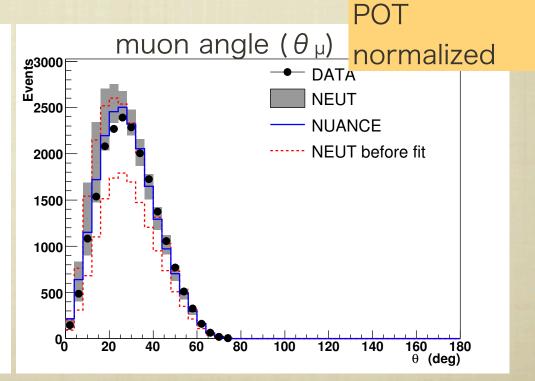
Phys. Rev. D 83, 012005 (2011)

Parameter	f_0	f_1	f_2	f_3	f_4	f_5
E_{ν} range (GeV)	0.25 - 0.5	0.5 - 0.75	0.75 - 1.0	1.0 - 1.25	1.25 - 1.75	1.75+

Distributions after fit

- Apply obtained rate normalization factors.
- Confirmed that the distribution well reproduce the data, and the errors become much smaller.





MRD-stopped

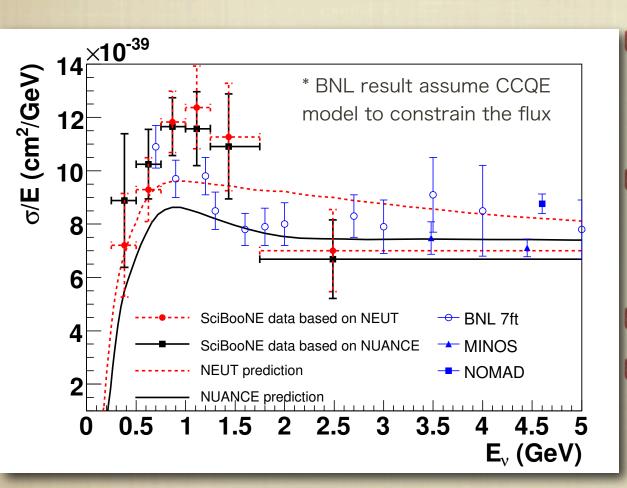
CC inclusive cross section

Extract CC inclusive cross section:

$$\sigma_i = f_i \cdot \langle \sigma_{CC}^{pred} \rangle_i = \frac{f_i \cdot \mathcal{N}_i^{pred} \cdot P_i}{\epsilon_i \cdot T \cdot \Phi_i}$$

T: number of target nucleon

Φ: total flux



- First measurement of CC-inclusive cross section on carbon in the 1 GeV region
- NEUT and NUANCE based cross-section are consistent.
- Covers up to ~ 3 GeV.
 - Consistent with MINOS,
 NOMAD and old BNL
 bubble chamber
 (deuterium) measurements

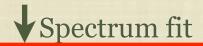
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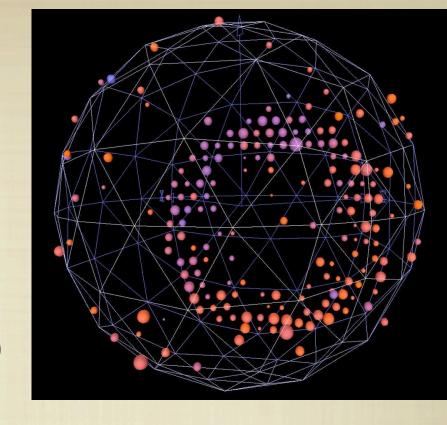
SB + MB Rec. E_v Prediction

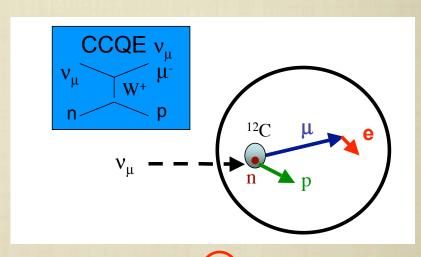
Advantage:

Direct fit for disappearance in SciBooNE and MiniBooNE. Correlation between the two constrain systematic error.

MiniBooNE reconstruction

- Employ same selection/reconstruction as used in previous MiniBooNE-only analysis (PRL **103**, 061802(2009))
- Select CC quasi-elastic (QE) (νn→μp) like events by requiring hits from muon and its decay electron.
- Reconstruct muon kinematics from the Cherenkov light yield.
- Reconstruct neutrino energy from muon kinematics, assuming CC-QE interaction.





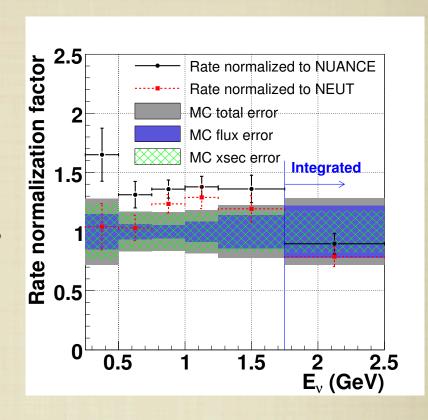
$$E_{\nu}^{rec} = \frac{m_p^2 - (m_n - E_B)^2 - m_{\mu}^2 + 2(m_n - E_B)E_{\mu}}{2(m_n - E_B - E_{\mu}) + p_{\mu}\cos\theta_{\mu}}$$

MiniBooNE prediction

Apply the rate normalization factor obtained by SciBooNE analysis to MiniBooNE.

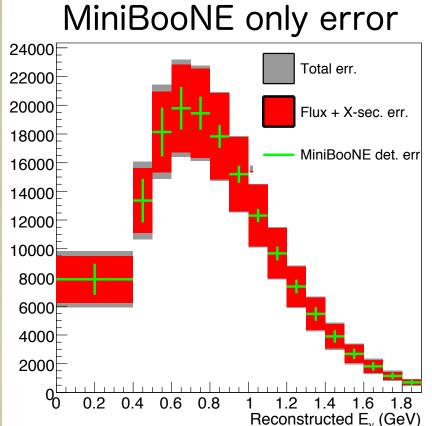
Systematic errors:

- Most of flux and cross section errors cancel by taking ratio between SciBooNE and MiniBooNE.
- Remaining errors:
 - Relative flux difference
 - Efficiency variation due to cross section model uncertainties.
 - MiniBooNE detector response errors.



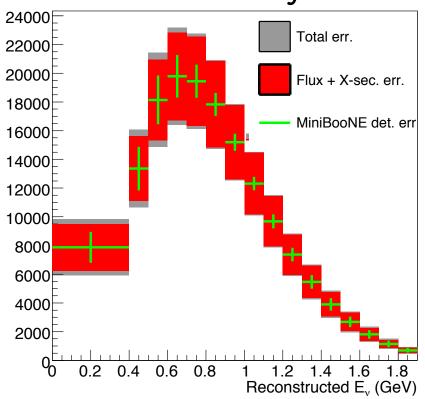
Carefully estimated these errors

MiniBooNE prediction

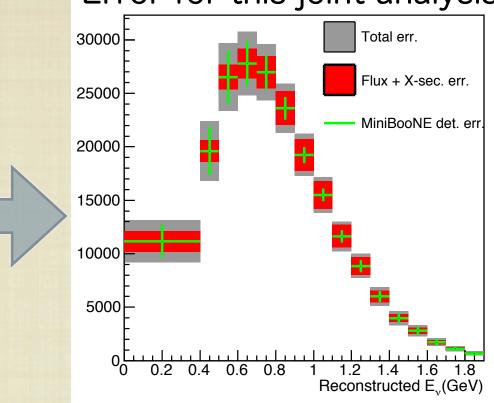


MiniBooNE prediction





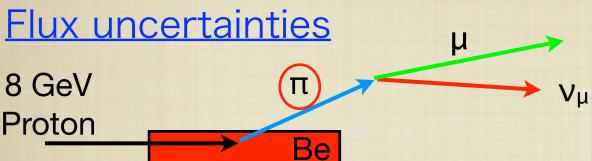
Error for this joint analysis



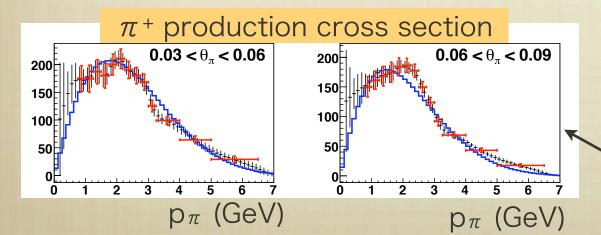
MiniBooNE prediction Error for this joint analysis MiniBooNE only error 24000 □ Total err. 30000 Total err. 22000 Fractional error Flux + X-sec. err. 20000 18000 Flux/X-sec and total Total err. MiniBooNE-only Flux/Xerror constrained by Flux + X-sec. err. sec and total error SciBooNE data MiniBooNE det. err. 10000 0.25 8000 0.2F 6000 4000 0.15 2000 MiniBooNE detector 0.1F response error 0.05 Reconstructed E. (GeV)

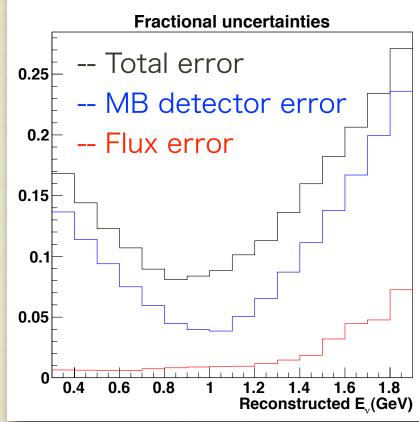
Successfully reduced flux and cross section errors to the same level of the MiniBooNE detector response errors.

Systematic uncertainties(1)



- Use HARP p-Be interaction measurement uncertainty for the error analysis.
- Become negligible after taking ratio between SciBooNE and MiniBooNE





-- Cross section used for MC production-- HARP data

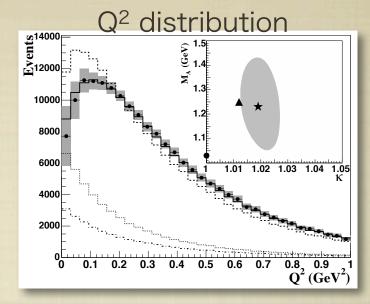
Spline interpolation of HARP data

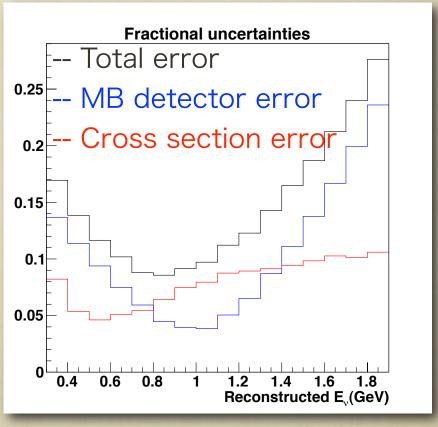
Systematic uncertainties (2)

Cross section uncertainties

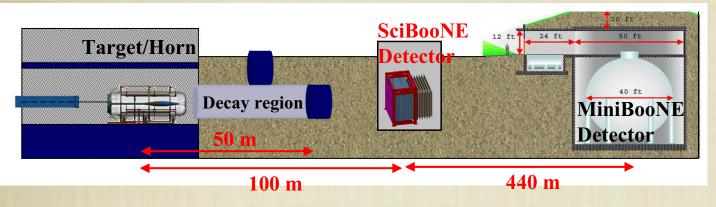
- Variation of Q² (muon angle) distribution can change relative acceptance.
 - SciBooNE: forward muon only
 - MiniBooNE: isotropic acceptance.
- The major source of the systematic error, together with the detector response error.

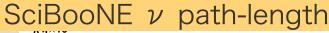
MiniBooNE CCQE sample

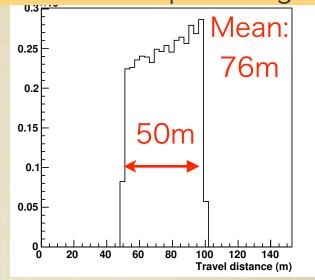




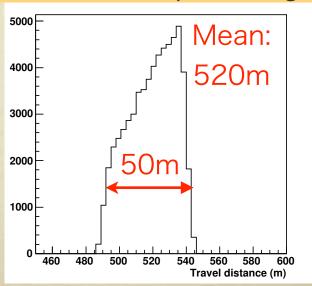
Predicting the oscillation signal





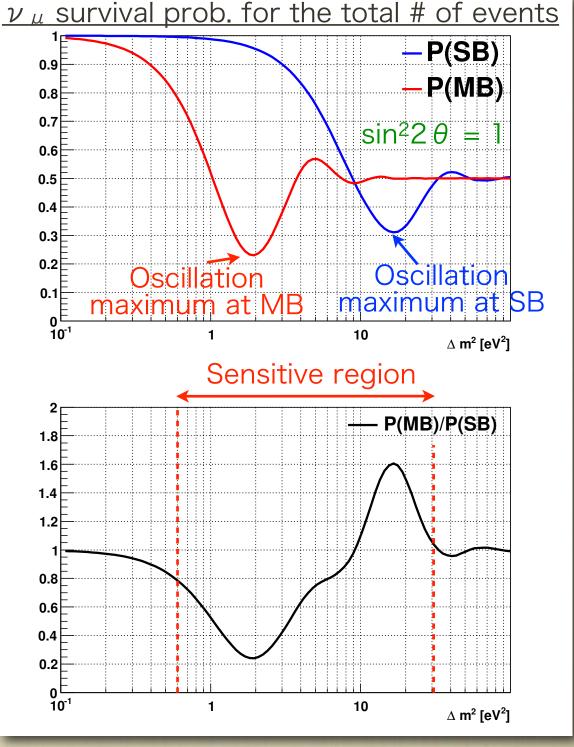


- Mean ν path-length for SciBooNE events: ~76m
- Mean ν path-length for MiniBooNE events: ~520m MiniBooNE ν path-length
- Each has 50m spread due to the finite length of the decay volume
- We take all the three effects into account:
 - Oscillation at SciBooNE
 - Oscillation at MiniBooNE
 - Smearing effect due to 50m spread



Oscillation probability

- General behavior
 - Oscillation reaches maximum at the first oscillation peak.
 - Then washes out at high Δm² by integrating over neutrino energy.
- Since we compare the MB flux with SB, P(MB)/P(SB) is the expected signal.
- Sensitive to oscillations at $0.5 < \Delta m^2 < 30 \text{ eV}^2$.



Oscillation fit

Test oscillation hypothesis between 2 flavors, and scan over $(\Delta m^2, \sin^2 2\theta)$ plane. $P(\nu_{\alpha} \rightarrow \nu_{\beta}) = \sin^2 2\theta \sin^2 \left(\frac{1.27\Delta m^2 [\text{eV}^2]L[\text{km}]}{E[\text{GeV}]}\right)$

Evaluate

$$\Delta \chi^2 = \chi^2$$
(each point) - χ^2 (best)

$$\chi^{2} = \sum_{jk} (M_{j}^{obs} - M_{j}^{pred}) V_{jk}^{-1} (M_{k}^{obs} - M_{k}^{pred})$$

Mobs: Data

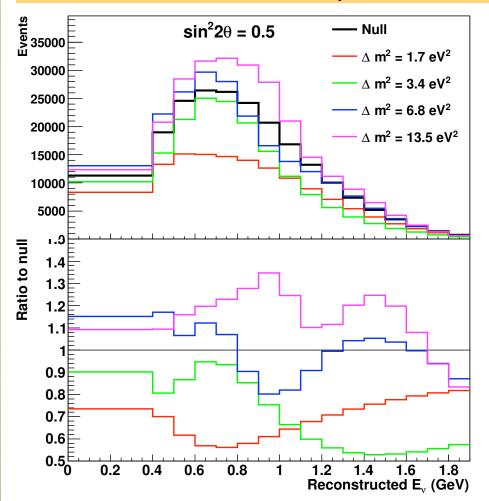
Mpred: Prediction

(function of osc. parameter)

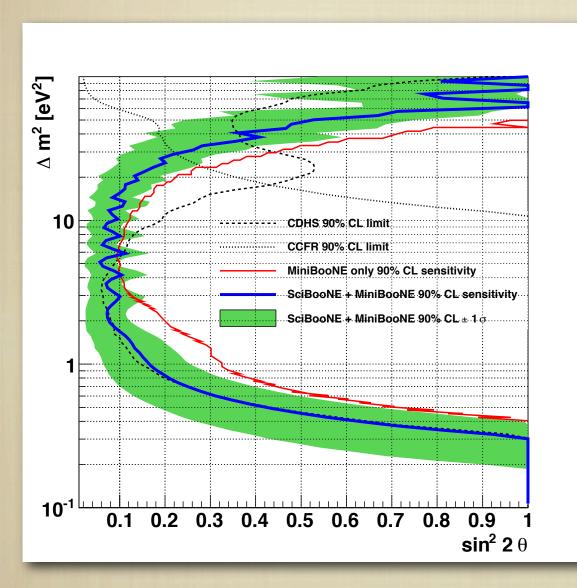
V: Covariance matrix

Use Feldman-Cousins method to find the confidence level for the obtained Δ χ² values.

MiniBooNE E_{ν} (rec) prediction



Sensitivity



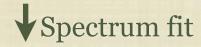
- Sensitivity reach to $\sin^2 2\theta \sim 0.1$ at $1 < \Delta m^2 < 20 \text{ eV}^2$
- Significantly improved from MiniBooNE-only analysis.
- Achieved world best sensitivity at
 0.5 < Δm² < 30 eV²

Analysis Overview

Two independent analyses

Spectrum fit

SciBooNE data



CC interaction rate measurement



MiniBooNE rec. E_v prediction



Oscillation Fit

MiniBooNE rec. E_v data

Advantage:

Decouple oscillation fit from constraint.

Observe the amount of constraint.

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Simultaneous fit

SB + MB Rec. E_v Data



Oscillation Fit

SB + MB Rec. E_v Prediction

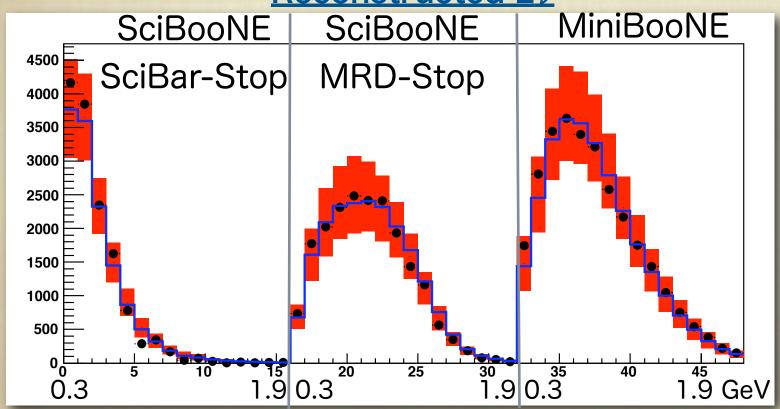
Advantage:

Direct fit for disappearance in SciBooNE and MiniBooNE. Correlation between the two constrain systematic error.

Simultaneous Fit

- Fit reconstructed E_{ν} distributions from SciBar-stopped, MRD-stopped and MiniBooNE samples simultaneously.
 - 16 bins/sample x 3 sample = 48 bins
- All bin-to-bin correlation is included into the fit.
 - Off-diagonal elements are strongly correlated.

Reconstructed E_V



- Fake Data
- MC with error(Diagonal part)
- * MiniBooNE distribution is scaled by ~1/7

Simultaneous Fit (cont'd)

- MC prediction is renormalized by the number of events in SciBooNE.
- Evaluate

$$\Delta \chi^2 = \chi^2 \text{(each point)} - \chi^2 \text{(best)}$$

$$\chi^2 = \sum_{i=1}^{BINS} (d_i - Np_i) M_{ij}^{-1} (d_j - Np_j)$$

di: Data

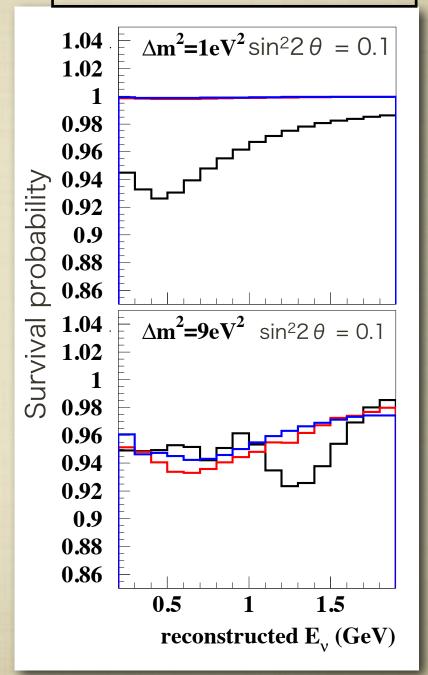
pi: Prediction (function of osc. parameter)

Mij: 48x48 covariance matrix

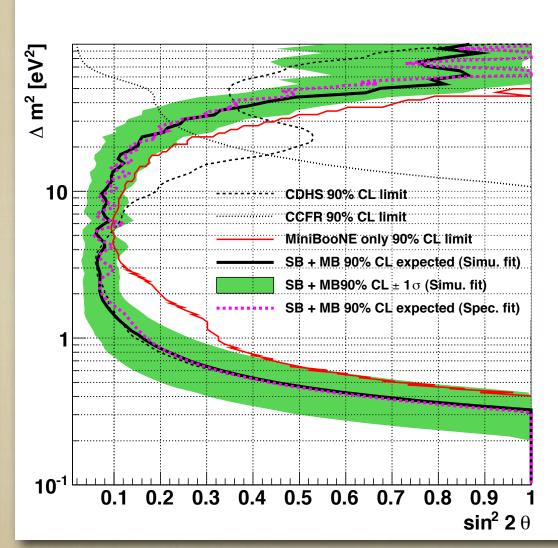
N: Renormalization factor

Again, Feldman-Cousins's method is used to determine the CLs.

- -- SciBooNE SciBar-stoped
- -- SciBooNE MRD-stopped
- -- MiniBooNE



Simultaneous fit sensitivity



- Sensitivities of the two analysis method are (roughly) same.
- Simultaneous fit sensitivity curve is smoother because of smaller binning effect than the spectrum fit analysis.

Results

Spectrum fit result

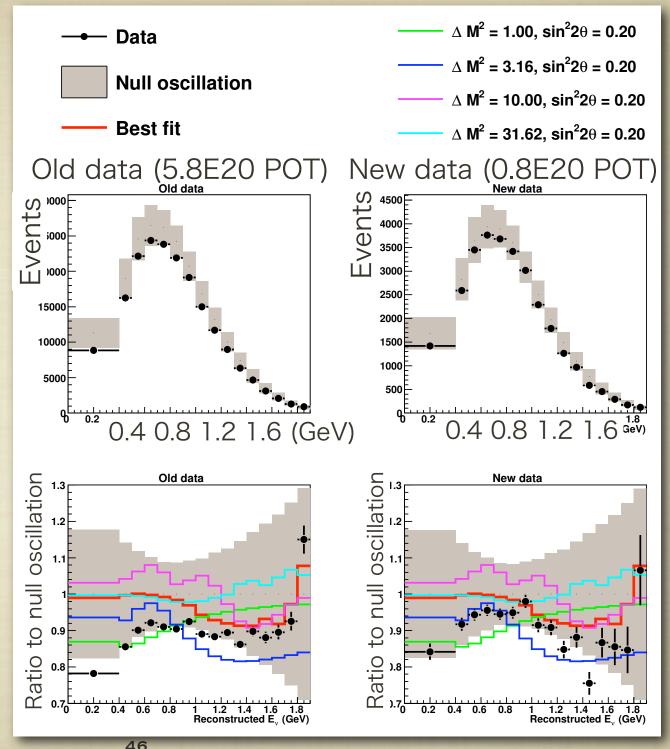
Fit both MiniBooNE new and old data

Best: $\Delta m^2 = 41.7 \text{ eV}^2$, $\sin^2 2\theta = 0.51$ $\chi^2(\text{null}) = 41.5/32(\text{DOF})$ $\chi^2(\text{best}) = 35.6/30(\text{DOF})$ $\Delta \chi^2 = \chi^2(\text{null}) - \chi^2(\text{best}) = 5.9$

 $\Delta \chi^2$ (90%CL, null) = 8.4 (estimated by simulation)

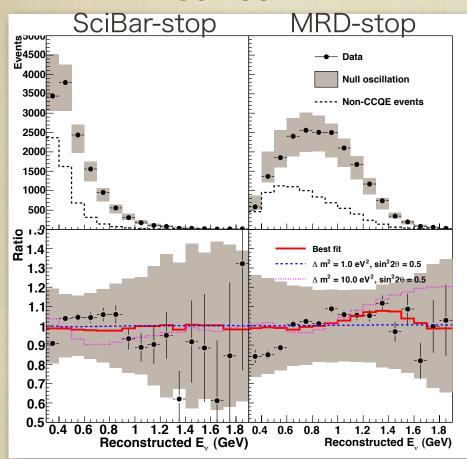
No significant oscillation signal observed.

Small data/MC discrepancy found, but doesn't match oscillation signature.



Simultaneous fit result

SciBooNE

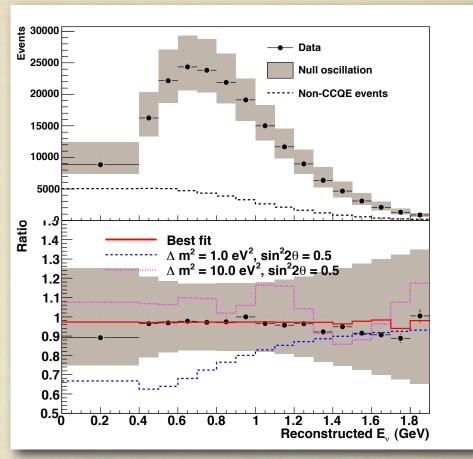


Best: $\Delta m^2 = 43.7 \text{ eV}^2$, $\sin^2 2\theta = 0.60$

$$\chi^{2}(\text{null}) = 45.1/48(\text{DOF})$$

 $\chi^{2}(\text{best}) = 39.5/46(\text{DOF})$
 $\Delta \chi^{2} = \chi^{2}(\text{null}) - \chi^{2}(\text{best}) = 5.6$

MiniBooNE

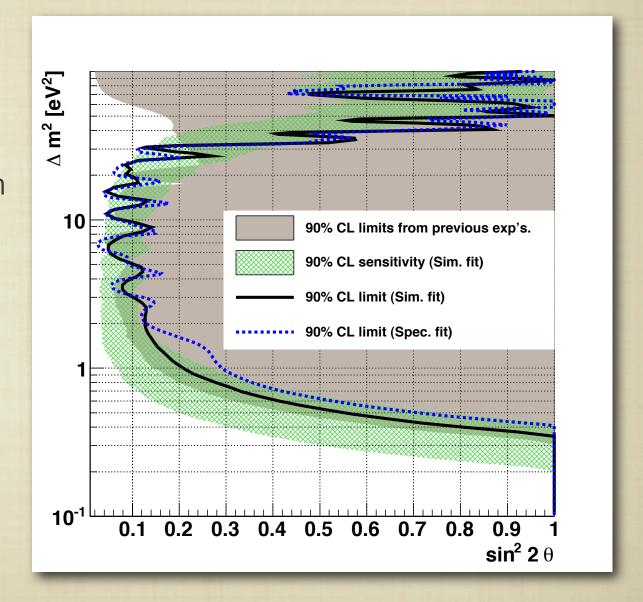


 $\Delta \chi^2$ (90%CL, null) = 9.3 (estimated by simulation)

No significant oscillation signal observed, too.

90% CL limit

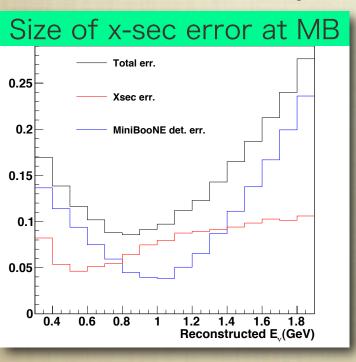
- The observed limits from both analyses are within the ±1 σ band.
 - Another support for null oscillation signal.
- World strongest limit at $10 < \Delta m^2 < 30 \text{ eV}^2$

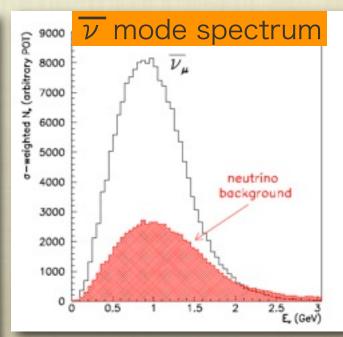


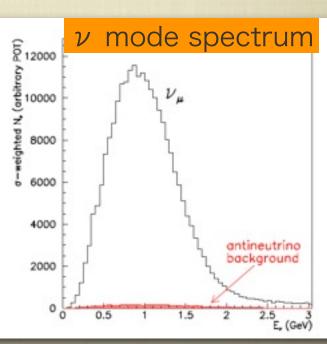
Discussions

- Possible Improvements:
 - Dominant uncertainty: neutrino x-section and MiniBooNE detector response.
 - Further analysis of SciBooNE (and MiniBooNE) data can reduce the cross section errors.
 - To reduce detector error, need identical detectors both at near and far sites.
- Muon antineutrino disappearance analysis

 Particularly interesting!
 - This analysis method directly applicable for anti-neutrino analysis.
 - Neutrino-mode result constrain "neutrino background", together with a direct measurement by MiniBooNE (arXiv:1102.164)







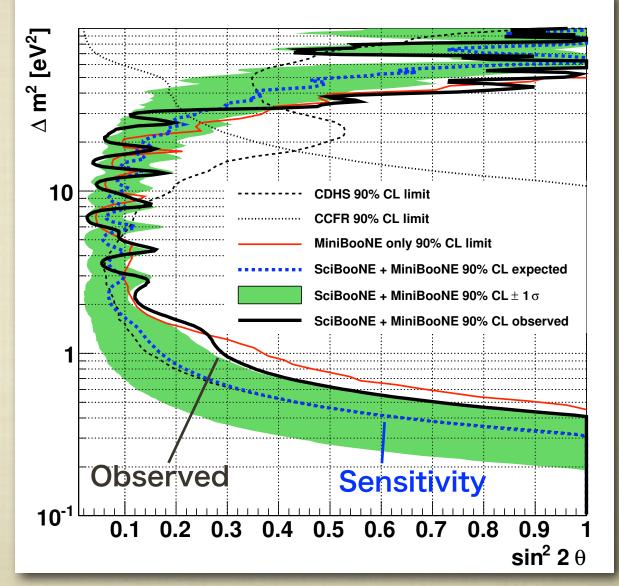
Conclusions

- A joint search for muon neutrino disappearance at
 Δm² ~ 1eV² with SciBooNE and MiniBooNE is presented.
- Two independent analyses performed; both showed consistent results.
 - Achieved the world best sensitivity at 0.5 < Δm² < 30 eV²</p>
 - No significant oscillation signal found
 - Set the best 90%CL limit at $10 < \Delta m^2 < 30 \text{ eV}^2$
- Preparing for publication of this result.
- Stay tuned for a forthcoming joint muon anti-neutrino disappearance analysis!

Backup Slides

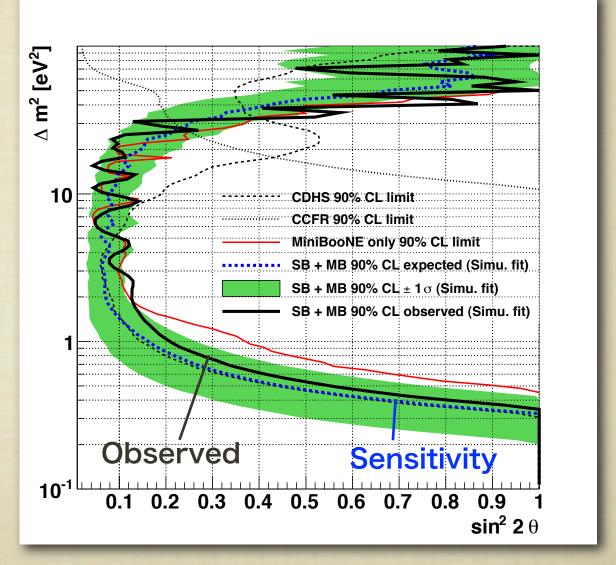
90% CL limit from spectrum fit

- The observed limits are within the $\pm 1 \sigma$ band.
 - Another support for null oscillation signal.
- World strongest limit at $10 < \Delta m^2 < 30 \text{ eV}^2$
 - Constrain sterile neutrino mixing parameters.



90% CL limit from simultaneous fit

- The observed limits are within the $\pm 1 \sigma$ band.
 - Another support for null oscillation signal.
- World strongest limit at $10 < \Delta m^2 < 30 \text{ eV}^2$
 - Constrain sterile neutrino mixing parameters.



List of systematic uncertainties

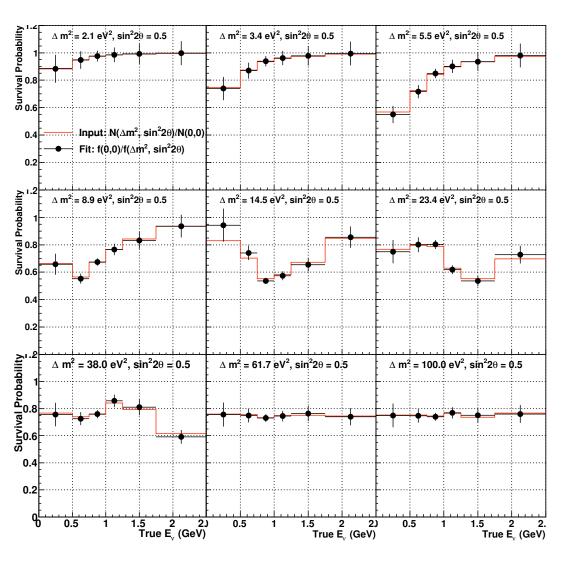
TABLE VIII. List of systematic uncertainties considered	TABLE VIII	List of	systematic	uncertainties	considered
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Catagori	Error Source	Variation	Dogarintian
Category			Description Sec. II B
	π^+/π^- production from p-Be interaction	Spline fit to HARP data [19]	
(:)	K^+/K^0 production from p-Be interaction	Tables VIII and IX in Ref. [21]	Sec. II B
(i)	Nucleon and pion interaction in Be/Al	Table XIII in Ref. [21]	Sec. II B
Flux	Horn current	±1 kA	Sec. II B
	Horn skin effect	Horn skin depth, ± 1.4 mm	Sec. II B
	Number of POT	$\pm 2\%$	Sec. II B
	Fermi surface momentum of carbon nucleus	$\pm 30~{ m MeV}$	Sec. III B 1
	Binding energy of carbon nucleus	$\pm 9~{ m MeV}$	Sec. III B 1
(ii)	CC - $QE M_A$	$\pm 0.22~{\rm GeV}$	Sec. III B 1
Neutrino	CC-QE κ	± 0.022	Sec. III B 1
interaction	$\text{CC-1}\pi\ M_A$	$\pm 0.28~{\rm GeV}$	Sec. III B 2
	$\text{CC-}1\pi Q^2 \text{ shape}$	Estimated from SciBooNE data	Sec. III B 2
	CC-coherent- π M_A	$\pm 0.28~{ m GeV}$	Sec. III B 3
	CC-multi- π M_A	$\pm 0.52~{\rm GeV}$	Sec. III B 4
	Δ re-interaction in nucleus	$\pm 100~\%$	Sec. III B 2
(iii)	Pion charge exchange in nucleus	$\pm 20~\%$	Sec. III B 5
Intra-nuclear	Pion absorption in nucleus	$\pm 35~\%$	Sec. III B 5
interaction	Proton re-scattering in nucleus	$\pm 10~\%$	Sec. III B 5
	NC/CC ratio	$\pm 20~\%$	Sec. III B 5
	PMT 1 p.e. resolution	±0.20	Sec. II D
	Birk's constant	$\pm 0.0023~\mathrm{cm/MeV}$	Sec. II D
(iv)	PMT cross-talk	± 0.004	Sec. II D
Detector	Pion interaction cross section in the detector material	$\pm 10~\%$	Sec. II D
response	dE/dx uncertainty	$\pm 3\%$ (SciBar,MRD), $\pm 10\%$ (EC)	Sec. II D
_	Density of SciBar	±1 %	Sec. II C
	Normalization of interaction rate at the EC/MRD	$\pm 20~\%$	Sec. III A
	Normalization of interaction rate at the surrounding materials	±20 %	Sec. III A

Rate normalization factors from SciBooNE spectrum fit

Energy region	ν_{μ} CC rate no	rmalization factor
(GeV)	NEUT	NUANCE
0.25 - 0.50	1.04 ± 0.20	1.65 ± 0.22
0.50 - 0.75	1.03 ± 0.11	1.31 ± 0.11
0.75 - 1.00	1.23 ± 0.08	1.36 ± 0.08
1.00 - 1.25	1.29 ± 0.10	1.38 ± 0.09
1.25 - 1.75	1.19 ± 0.11	1.36 ± 0.12
1.75 -	0.79 ± 0.08	0.90 ± 0.09

Test of SB spectrum fit with oscillation effects



Black points: fit result

Red lines: input value